

More Practice: Geometric Sequences

KEY

What are the next 3 terms in the sequence and find the common ratio for the sequence:

1. $6, 12, 24, \underline{48}, \underline{96}, \underline{192}$
2. $6, 1.8, 0.54, \underline{0.162}, \underline{0.0486}, \underline{0.01458}$
3. $5, -10, 20, \underline{-40}, \underline{80}, \underline{-160}$

$$\text{Common ratio} = 2$$

$$\text{Common ratio} = 0.3$$

$$\text{Common ratio} = -2$$

Write the first four terms of the given sequence:

4. $a_n = 0.5 \cdot 2^{n-1}$ $0.5, 1, 2, 4$
5. $a_n = 3 \cdot (0.1)^{n-1}$ $3, 0.3, 0.03, 0.003$

Write the explicit formula for the given sequences:

6. $\overbrace{7, 49, 343, \dots}^{\times 7} \quad a_n = 7 \cdot 7^{n-1}$
7. $\overbrace{\frac{1}{63}, \frac{1}{21}, \frac{1}{7}, \dots}^{\times 3} \quad a_n = \frac{1}{63} \cdot 3^{n-1}$
8. $0.46, 0.92, 1.84, \dots \quad a_n = 0.46 \cdot 2^{n-1}$

Find the given term of the geometric sequence.

$$9. a_1 = 3, r = 4, n = 8 \quad a_8 = 3 \cdot 4^{(8-1)} = 3 \cdot 4^7 = 3 \cdot 16,384 = 49,152$$

$$10. a_1 = 0.6, r = 3, n = 17 \quad a_{17} = 0.6 \cdot 3^{(17-1)} = 0.6 \cdot 3^{16} = 0.6(43,046,721) \\ = 25,828,032.6$$

$$11. a_1 = 5, r = -6, n = 12 \quad a_{12} = 5(-6)^{(12-1)} = 5(-6)^{11} = 5 \cdot (-362,797,056) \\ = -1,813,985,280$$

The given number is which number in the given sequence?

$$12. 20971520, a_n = 5(4)^{n-1} \quad 4194304 = 4^{n-1} \\ \underline{20971520} = \underline{5}(\underline{4})^{n-1} \quad n-1 = \log_4 4194304 = \frac{\log 4194304}{\log 4} = 11 \\ \text{so } n-1 = 11, \quad n = 12$$

$$13. 11468.8, a_n = 0.7(2)^{n-1} \quad 11468.8 = 0.7(2)^{n-1} \quad 16384 = 2^{n-1} \\ n-1 = \log_2 16384 = \frac{\log 16384}{\log 2} = 14 \quad n-1 = 14 \\ \text{so } n-1 = 14, \quad n = 15$$